

Use $\log_2 3 \approx 1.5850$ and $\log_2 5 \approx 2.3219$ to approximate the value of each expression.

$$1. \log_2 25 = \log_2 5 + \log_2 5 = 4.6438$$

$$3. \log_2 \frac{3}{5} = \log_2 3 - \log_2 5 =$$

$$5. \log_2 15 = \log_2 3 + \log_2 5 =$$

$$7. \log_2 75 = \log_2 5^2 + \log_2 3 =$$

$$2 \log_2 5 + \log_2 3 =$$

$$9. \log_2 \frac{1}{3} = \log_2 3^{-1} = -1 \log_2 3 =$$

$$2. \log_2 27 = \log_2 3^3 = 3 \log_2 3 = 4.755$$

$$4. \log_2 \frac{5}{3} = \log_2 5 - \log_2 3 =$$

$$6. \log_2 45 = \log_2 3^2 + \log_2 5 = 2 \log_2 3 + \log_2 5 =$$

$$8. \log_2 0.6 = \log_2 3 - \log_2 5 =$$

$$10. \log_2 \frac{9}{5} = \log_2 3^2 - \log_2 5 = 2 \log_2 3 - \log_2 5$$

$$11. \log_{10} 27 = 3 \log_{10} x$$

$$\log_{10} 27 = \log_{10} x^3$$

$$27 = x^3$$

$$x = 3$$

$$12. 3 \log_7 4 = 2 \log_7 b$$

$$(4^3)^{\frac{1}{2}} = (b^2)^{\frac{1}{2}}$$

$$4^{3/2} = b$$

$$b = 8$$

$$4^{\frac{3}{2}} = (4^{\frac{1}{2}})^3 = 2^3 = 8$$

13. $\log_4 5 + \log_4 x = \log_4 60$

$$5x = 60$$

$$x = 12$$

14. $\log_6 2c + \log_6 8 = \log_6 80$

$$16c = 80$$

$$c = 5$$

15. $\log_5 y - \log_5 8 = \log_5 1$

$$\frac{y}{8} = 1$$

$$y = 8$$

16. $\log_2 q - \log_2 3 = \log_2 7$

$$\frac{q}{3} = 7$$

$$q = 21$$

$$17. \log_9 4 + 2 \log_9 5 = \log_9 w$$

$$4 \cdot 25 = w$$

$$w = 100$$

$$18. 3 \log_8 2 - \log_8 4 = \log_8 b$$

$$\frac{8}{4} = b$$

$$2 = b$$

$$19. \log_{10} x + \log_{10} (3x - 5) = \log_{10} 2$$

$$x(3x - 5) = 2$$

$$3x^2 - 5x = 2$$

$$3x^2 - 5x - 2 = 0$$

$$\frac{5 \pm \sqrt{25 - 4(3)(-2)}}{6}$$

$$= \frac{5 \pm \sqrt{49}}{6} = \frac{5 \pm 7}{6}$$

$$= 2 \text{ or } -\frac{1}{6}$$

$$20. \log_4 x + \log_4 (2x - 3) = \log_4 2$$

$$x(2x - 3) = 2$$

$$2x^2 - 3x = 2$$

$$2x^2 - 3x - 2 = 0$$

$$(2x + 1)(x - 2) = 0$$

$$x = -\frac{1}{2} \text{ or } 2$$

$$21. \log_3 d + \log_3 3 = 3$$

$$3d = 3$$

$$d = 1$$

$$22. \log_{10} y - \log_{10} (2 - y) = 0$$

$$(2-y) \cdot \frac{y}{2-y} = 0 \quad \cdot (2-y)$$

$$y = 0$$

$$23. \log_2 s + 2 \log_2 5 = 0$$

$$s \cdot 25 = 0$$

$$s = 0$$

$$24. \log_2 (x + 4) - \log_2 (x - 3) = 3$$

$$\frac{x+4}{x-3} = 3$$

$$x + 4 = 3x - 9$$

$$13 = 2x$$

$$6.5 = x$$

25. $\log_4 (n + 1) - \log_4 (n - 2) = 1$

$$\frac{n+1}{n-2} = 1$$

$$n+1 = n-2$$

$$1 = -2$$

no solution

26. $\log_5 10 + \log_5 12 = 3 \log_5 2 + \log_5 a$

$$10 \cdot 12 = 2^3 \cdot a$$

$$120 = 8a$$

$$15 = a$$

More rules for logarithms

$\ln x$ means $\log_e x$ (\ln is natural log)

exponents	logarithms
(All laws apply for any positive a , b , x , and y .)	
$x = b^y$	is the same as $y = \log_b x$
$b^0 = 1$	$\log_b 1 = 0$
$b^1 = b$	$\log_b b = 1$
$b^{(\log_b x)} = x$	$\log_b b^x = x$
$b^x b^y = b^{x+y}$	$\log_b(xy) = \log_b x + \log_b y$
$b^x \div b^y = b^{x-y}$	$\log_b(x/y) = \log_b x - \log_b y$
$(b^x)^y = b^{xy}$	$\log_b(x^y) = y \log_b x$
	$(\log_a b) (\log_b a) = \log_a a = 1$
	$\log_b x = (\log_a x) / (\log_a b)$
	$\log_b a = 1 / (\log_a b)$

$$5^{x+1} = 625$$

$$\log_5 5^{x+1} = \log_5 625$$

$$x+1 = \log_5 625$$

$$x+1 = 4$$

$$\begin{array}{r} -1 \quad -1 \end{array}$$

$$x = 3$$

$$2^{x-4} = 3$$

$$\log_2 2^{x-4} = \log_2 3$$

$$x-4 = \log_2 3$$

$$x-4 = 1.58$$

$$\begin{array}{r} +4 \quad +4 \end{array}$$

$$x = 5.58$$

$$\log_5(2x + 3) = 3$$

$$b^{(\log_b x)} = x$$

$$5^{\log_5(2x+3)} = 5^3$$

$$2x + 3 = 125$$

$$\begin{array}{r} -3 \quad -3 \end{array}$$

$$2x = 122$$

$$x = 61$$

$$\log_4(3x - 5) = 0$$

$$4^{\log_4(3x-5)} = 4^0$$

$$3x - 5 = 1$$

$$\begin{array}{r} +5 \quad +5 \end{array}$$

$$3x = 6$$

$$x = 2$$